

# JEE Mains 2024 31 January Shift 1

## Question Paper

According to the initial views of students who took the JEE Main January 31 Shift 1 exam, the general difficulty of the paper was moderate. Students noted that the Mathematics session was challenging and lengthy. The physics component was said to be easy but challenging. Students rated the chemistry portion as easy. Students also claimed that the Chemistry section contained more NCERT-based questions than the Physics section, which contained mostly formula-based questions.

Candidates can find memory-based questions for each subject on the JEE Mains 2024 31 Jan paper Shift 1 below.

### Physics

Q. If two charges  $Q$  and  $3Q$  are kept in a line separated by a distance  $R$ , the electric field is zero at a distance  $x$  from origin  $O$ . Find the value of  $x$ .

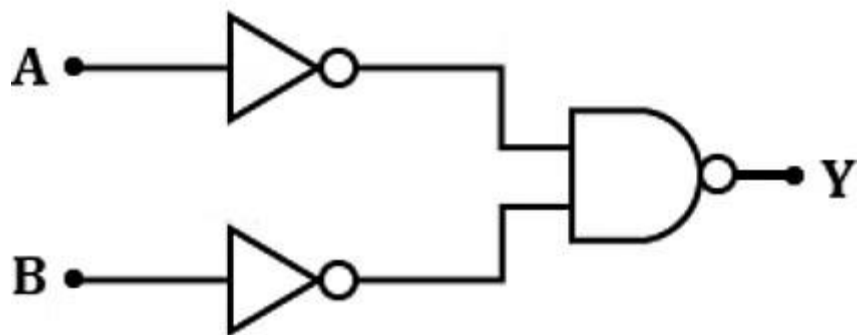
Q. A pulley is placed on top of a triangular surface such that it forms  $53^\circ$  and  $37^\circ$  with the horizontal. The pulley carries two blocks of masses  $M$  and  $m$  on the  $53^\circ$  incline and  $37^\circ$  incline respectively. If  $M = 10$  kg has an acceleration of  $2$  m/s<sup>2</sup> in the direction of the  $53^\circ$  incline plane, then find the mass  $m$ .

Q. If the stopping potential is  $8$  V for incident light with wavelength  $\lambda$  and it is  $2$  V for a wavelength of  $3\lambda$ , then find the threshold wavelength.

Q. If the mass defect in a nuclear reaction is  $0.4$  gm, then find the  $Q$ -value of the reaction.

Q. If the percentage error in measuring the length and diameter of a wire is  $0.1\%$  each, then find the percentage error of the resistance of the wire.

Q. What is the logic gate equivalent to the given logic circuit?



Q. Which of the following compounds is white in colour?

- i.  $\text{ZnSO}_4$
- ii.  $\text{CuSO}_4$
- iii.  $\text{FeSO}_4$
- iv.  $\text{FeCl}_3$

Q. On which of the following factors does the electrical conductivity of an electrolytic cell does not depend?

- i. Concentration of electrolyte
- ii. Amount of electrolyte added
- iii. Temperature
- iv. Nature of electrode

Q. A ball dropped from height  $H$  rebounds up to height  $h$  after colliding with a horizontal surface. If the coefficient of restitution for collision is  $e = 1/2$ , then find  $H/h$ .

## Chemistry

Q. Which of the following options contain amphoteric oxide(s) only?

- i.  $\text{SnO}_2$  and  $\text{SiO}$
- ii.  $\text{SiO}_2$
- iii.  $\text{SnO}_2$  and  $\text{PbO}_2$
- iv.  $\text{CO}$  and  $\text{SiO}$

Q. Find out the final product C for the reaction:

$\text{CH}_3\text{--CH}_2\text{--CH}_2\text{--Br} \rightarrow$  (in presence of alcoholic  $\text{KOH}$ , heat)  $\rightarrow$  Product A

Product A  $\rightarrow$  (in presence of  $\text{HBr}$ )  $\rightarrow$  Product B

Product B  $\rightarrow$  (in presence of aqueous  $\text{KOH}$ )  $\rightarrow$  Product C

Q. How many of the following compounds have  $sp^3$  hybridized central atom?  
 $H_2O$ ,  $NH_3$ ,  $SiO_2$ ,  $SO_2$ ,  $CO$  and  $BF_3$

Q. Assertion(A): Noble gases have very high boiling points.

Reason(R): Noble gases have strong dispersion forces. Hence, they liquefy at low temperatures and hence they have a high boiling point.

- Both A and R are true and R is the correct explanation of A.
- Both A and R are true and R is not the correct explanation of A.
- Both A and R are false.
- A is true but R is false.

Q. Assertion: The  $pK$  value of phenol is 10.0 while that of ethanol is 15.9.

Reason: Ethanol is a stronger acid than phenol.

- Both A and R are true and R is the correct explanation of A.
- Both A and R are true and R is not the correct explanation of A.
- Both A and R are false.
- A is true but R is false.

Q. The adsorption principle is used in

- Distillation
- Differential Extraction
- Chromatography
- Vacuum Distillation

Q. How many of the following can be used as electrodes in batteries?

- Zinc
- Zinc - Mercury amalgam
- Lead
- Graphite

### Mathematics

Q. If the system of linear equation  $x - 2y + z = -4$ ,  $2x + \alpha y + 3z = 5$  &  $3x - y + \beta z = 3$  has infinitely many solutions then find the value of  $12\alpha + 13\beta$ .

Q. ABCD is a parallelogram where  $A(\alpha, \beta)$ ,  $B(1,0)$ ,  $C(\gamma, \delta)$ , and  $D(3,2)$  and  $AB = \sqrt{10}$ . Find the value of  $2(\alpha + \beta + \gamma + \delta)$ .

Q.  $A = \{1, 2, 3, 4\}$ ,  $R = \{(1, 2), (2, 3), (2, 4)\}$ ,  $R \subseteq S$  and S is an equivalence relation, then the minimum number of elements to be added to R is n. Find the value of n.

Q. Let S be the set of positive integral value of a for which

$$[(ax^2 + 2(a+1)x + 9a + 4) / (x^2 + 8x + 32)] < 0 \quad \forall x \in \mathbb{R}.$$

Find the number of elements in S.

Q. The distance of the point Q(0,2,-2) from the line passing through the point P(5,-4,3) and perpendicular to the line  $r = (-3i + 2k) + \lambda(2i + 3j + 5k)$ ,  $\lambda \in \mathbb{R}$  and  $r = (i - 2j + k) + \mu(-i + 3j + 2k)$ ,  $\mu \in \mathbb{R}$  is?

Q. If one of the diameters of the circle  $x^2 + y^2 - 10x + 4y + 13 = 0$  is a chord of another circle and whose center is the point of intersection of the lines  $2x + 3y = 12$  and  $3x - 2y = 5$ . then the radius of the circle is?

Q. An urn contains 15 red, 10 white, 60 orange, and 15 green balls. If 2 balls are taken with replacement, find the probability 1 ball is red and the other ball is white.

Q4.  $\lim_{x \rightarrow 0} [(e^{2\sin x} - 2|\sin x| - 1) / x^2] = ?$

Q. If three vectors are:

$$a = 3i + j - 2k$$

$$b = 4i + j + 7k$$

$$c = i - 3j + 4k$$

If p is a vector such that  $p \times b = c \times b$  and  $p \cdot a = 0$ , then find  $p \cdot (i - j - k)$ .

Q. Find the solution of the differential equation  $y \, dy/dx = x(\log x - \log y + 1)$ ,  $x > 0$ ,  $y > 0$  and passes through (e, 1).

Q.  $f(x) = (4x + 3)/(6x - 4)$  and  $g(x) = f(f(x))$ , then find  $g(g(g(x)))$ .

Q. For  $\alpha, \beta, \gamma \neq 0$ , if  $\sin^{-1}\alpha + \sin^{-1}\beta + \sin^{-1}\gamma = \pi$  and  $(\alpha + \beta + \gamma)(\alpha - \gamma + \beta) = 3\alpha\beta$ , then find the value of  $\gamma$ .

Q. If  $|a| = 1$ ,  $|b| = 4$  and  $a \cdot b = 2$ . Also,  $c = (3a \times b) - b$  and  $\alpha$  is the angle between b and c, then what is the value of  $192 \sin^2 \alpha$ ?